

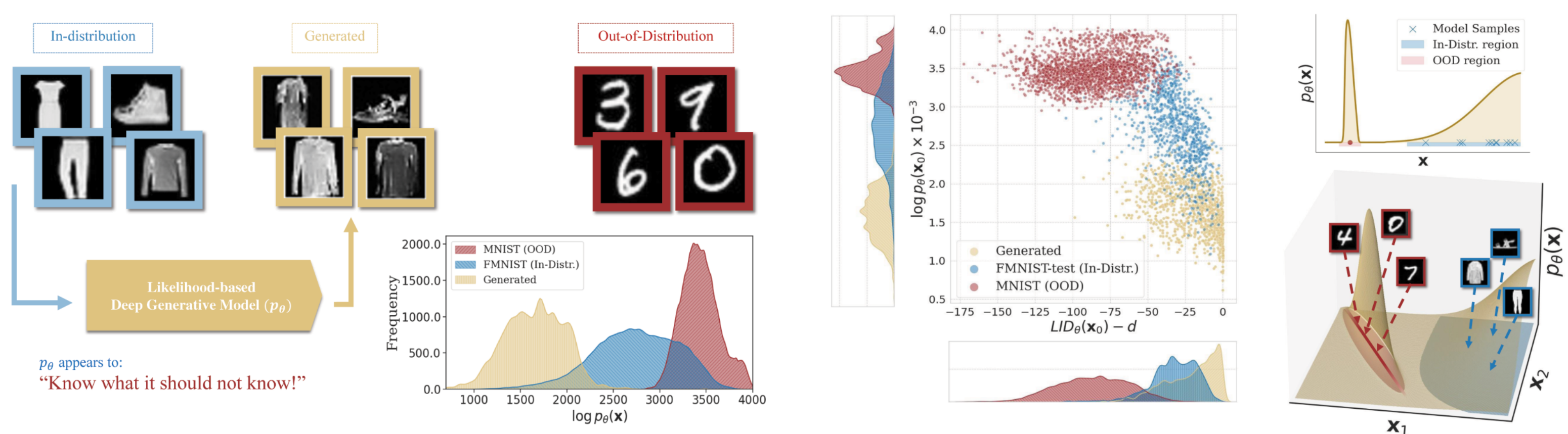
# Explaining the Out-of-Distribution Detection Paradox through Likelihood Peaks

Explaining a popular paradox in deep generative models from a manifold learning perspective, leading to enhanced reliability of generative models in detecting out-of-distribution data.

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## PROJECT SUMMARY

Likelihood-based deep generative models (DGGMs) commonly exhibit a puzzling behaviour: when trained on a relatively complex dataset, they assign higher likelihood values to out-of-distribution (OOD) data from simpler sources. Adding to the mystery, OOD samples are never generated by these DGGMs despite having high likelihoods. This two-pronged paradox has yet to be conclusively explained, making likelihood-based OOD detection unreliable. Our primary observation is that high-likelihood regions will not be generated if they contain minimal probability mass, which can occur if the density is sharply peaked. We demonstrate how this seeming contradiction of large densities yet low probability mass can occur on data confined to low dimensional manifolds. We also show that this scenario can be identified through local intrinsic dimension (LID) estimation, and propose a method for OOD detection which pairs the likelihoods and LID estimates obtained from a pre-trained DGGM. Moreover, we provide an efficient method for estimating LID from a normalizing flow model, improving upon existing estimators, and enabling state-of-the-art OOD detection performance with respect to comparable flow-based benchmarks.

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